

Duprez, Michel; Hélié, Romane; Privat, Yannick; Vauchelet, Nicolas
Optimization of spatial control strategies for population replacement, application to *Wolbachia*. (English) [Zbl 1471.92250](#)
ESAIM, Control Optim. Calc. Var. 27, Paper No. 74, 30 p. (2021).

Summary: In this article, we are interested in the analysis and simulation of solutions to an optimal control problem motivated by population dynamics issues. In order to control the spread of mosquito-borne arboviruses, the population replacement technique consists in releasing into the environment mosquitoes infected with the *Wolbachia* bacterium, which greatly reduces the transmission of the virus to the humans. Spatial releases are then sought in such a way that the infected mosquito population invades the uninfected mosquito population. Assuming very high mosquito fecundity rates, we first introduce an asymptotic model on the proportion of infected mosquitoes and then an optimal control problem to determine the best spatial strategy to achieve these releases. We then analyze this problem, including the optimality of natural candidates and carry out first numerical simulations in one dimension of space to illustrate the relevance of our approach.

MSC:

- [92D25](#) Population dynamics (general)
- [92D45](#) Pest management
- [49K15](#) Optimality conditions for problems involving ordinary differential equations
- [65K10](#) Numerical optimization and variational techniques

Cited in 1 Document

Keywords:

[reaction-diffusion equation](#); [optimal control](#); [second order optimality conditions](#)

Software:

[Ipopt](#)

Full Text: [DOI](#) [arXiv](#)

References:

- [1] L. Almeida, M. Duprez, Y. Privat and N. Vauchelet, Mosquito population control strategies for fighting against arboviruses. *Math. Biosci. Eng.* 16 (2019) 6274. · [Zbl 1470.92276](#)
- [2] L. Almeida, Y. Privat, M. Strugarek and N. Vauchelet, Optimal releases for population replacement strategies: application to *wolbachia*. *SIAM J. Math. Anal.* 51 (2019) 3170-3194. · [Zbl 1421.92029](#)
- [3] L. Almeida, A. Haddon, C. Kermorvant, A. Léculier, Y. Privat, M. Strugarek, N. Vauchelet and J.P. Zubelli, Optimal release of mosquitoes to control dengue transmission. *ESAIM: Procs* 67 (2020) 16-29. · [Zbl 1447.92389](#)
- [4] N.H. Barton and M. Turelli, Spatial waves of advance with bistable dynamics: cytoplasmic and genetic analogues of Allee effects. *Am. Natur.* 178 (2011) E48-E75.
- [5] L. Beal, D. Hill, R. Martin and J. Hedengren, Gekko optimization suite. *Processes* 6 (2018) 106.
- [6] P.-A. Bliman, Feedback control principles for biological control of dengue vectors. 18th European Control Conference (ECC), arXiv preprint [arXiv:1903.00730](#) (2019).
- [7] K. Bourtzis, *Wolbachia*-based technologies for insect pest population control, in *Transgenesis and the management of vector-borne disease*. Springer (2008) 104-113.
- [8] D.E. Campo-Duarte, O. Vasilieva, D. Cardona-Salgado and M. Svinin, Optimal control approach for establishing *wolbachia* infection among wild *aedes aegypti* populations. *J. Math. Biol.* 76 (2018) 1907-1950. · [Zbl 1390.92133](#)
- [9] E.D. Conway and J.A. Smoller, A comparison technique for systems of reaction-diffusion equations. *Commun. Partial Differ. Equ.* 2 (1977) 679-697. · [Zbl 0386.35003](#)
- [10] G.L.C. Dutra, L.M.B. dos Santos, E.P. Caragata, J.B.L. Silva, D.A.M. Villela, R. Maciel-de Freitas and L. Andrade Moreira, From Lab to Field: the influence of urban landscapes on the invasive potential of *Wolbachia* in Brazilian *Aedes aegypti* mosquitoes. *PLoS Negl Trop Dis* 9 (2015).
- [11] V.A. Dyck, J. Hendrichs and A. Robinson, Sterile insect technique: principles and practice in area-wide integrated pest

management. Springer (2006).

- [12] L.C. Evans, Vol. 19 of Partial differential equations. American Mathematical Society (AMS), Providence, RI (2010), 2nd edn. · [Zbl 1194.35001](#)
- [13] J.Z. Farkas and P. Hinow, Structured and unstructured continuous models for wolbachia infections. *Bull. Math. Biol.* 72 (2010) 2067-2088. · [Zbl 1201.92044](#)
- [14] A. Fenton, K.N. Johnson, J.C. Brownlie and G.D.D. Hurst, Solving the wolbachia paradox: modeling the tripartite interaction between host, wolbachia, and a natural enemy. *Am. Natur.* 178 (2011) 333-342.
- [15] D.A. Focks, D.G. Haile, E. Daniels and G.A. Mount, Dynamic life table model for *Aedes aegypti* (Diptera: Culicidae): analysis of the literature and model development. *J. Med. Entomol.* 30 (1993) 1003-1017.
- [16] G. Fu, R. Lees, D. Nimmo, D. Aw, L. Jin, P. Gray, T. Berendonk, H. White-Cooper, S. Scaife, H.K. Phuc, et al., Female-specific flightless phenotype for mosquito control. *Proc. Natl. Acad. Sci.* 107 (2010) 4550-4554.
- [17] J. Heinrich and M. Scott, A repressible female-specific lethal genetic system for making transgenic insect strains suitable for a sterile-release program. *Proc. Natl. Acad. Sci.* 97 (2000) 8229-8232.
- [18] J.-B. Hiriart-Urruty and C. Lemaréchal, Convex analysis and minimization algorithms. I. Vol. 305 of Grundlehren der Mathematischen Wissenschaften
- [19] H. Hughes and N.F. Britton, Modelling the use of wolbachia to control dengue fever transmission. *Bull. Math. Biol.* 75 (2013) 796-818. · [Zbl 1273.92034](#)
- [20] K. Le Balc'h Null-controllability of two species reaction-diffusion system with nonlinear coupling: a new duality method. *SIAM J. Control Optim.* 57 (2019) 2541-2573. · [Zbl 1461.35124](#)
- [21] X.J. Li and J.M. Yong, Necessary conditions for optimal control of distributed parameter systems. *SIAM J. Control Optim.* 29 (1991) 895-908. · [Zbl 0733.49025](#)
- [22] I. Mazari, D. Ruiz-Balet and E. Zuazua, Constrained control of bistable reaction-diffusion equations: gene-flow and spatially heterogeneous models. Preprint (2020).
- [23] I. Mazari, G. Nadin and A.I. Toledo Marrero Optimization of the total population size with respect to the initial condition in reaction-diffusion equations. Work in progress (2021).
- [24] T.Y. Miyaoka, S. Lenhart and J.F.C.A. Meyer, Optimal control of vaccination in a vector-borne reaction-diffusion model applied to zika virus. *J. Math. Biol.* 79 (2019) 1077-1104. · [Zbl 1416.35136](#)
- [25] G. Nadin and A.I. Toledo Marrero On the maximization problem for solutions of reaction-diffusion equations with respect to their initial data. *Math. Model. Nat. Phenom.* 15 (2020) 71. · [Zbl 1469.35025](#)
- [26] T. Ouyang and J. Shi, Exact multiplicity of positive solutions for a class of semilinear problem II. *J. Differ. Equ.* 158 (1999) 94-151. · [Zbl 0947.35067](#)
- [27] B. Perthame, Parabolic equations in biology. Growth, reaction, movement and diffusion. Springer, Cham (2015). · [Zbl 1333.35001](#)
- [28] J. Schraiber, A. Kaczmarczyk, R. Kwok, M. Park, R. Silverstein, F. Rutaganira, T. Aggarwal, M. Schwemmer, C. Hom, R. Grosberg, et al., Constraints on the use of lifespan-shortening Wolbachia to control dengue fever. *J. Theor. Biol.* 297 (2012) 26-32. · [Zbl 1336.92085](#)
- [29] J. Simon, Compact sets in the space $L^p(0, T; B)$. *Ann. Mat. Pura Appl.* 146 (1987) 65-96. · [Zbl 0629.46031](#)
- [30] S. Sinkins, Wolbachia and cytoplasmic incompatibility in mosquitoes. *Insect Biochem. Mol. Biol.* 34 (2004) 723-729.
- [31] B. Stoll, H. Bossin, H. Petit, J. Marie and M.A. Cheong Sang Suppression of an isolated population of the mosquito vector *aedes polynesiensis* on the atoll of tetiaroa, french polynesia, by sustained release of wolbachia-incompatible male mosquitoes. In Conference: ICE - XXV International Congress of Entomology, At Orlando, Florida, USA (2016).
- [32] M. Strugarek and N. Vauchelet, Reduction to a single closed equation for 2-by-2 reaction-diffusion systems of Lotka-Volterra type. *SIAM J. Appl. Math.* 76 (2016) 2060-2080. · [Zbl 1355.35108](#)
- [33] M. Strugarek, N. Vauchelet and J.P. Zubelli, Quantifying the survival uncertainty of wolbachia-infected mosquitoes in a spatial model. *Math. Biosci. Eng.* 15 (2018) 961-991. · [Zbl 1406.92522](#)
- [34] D. Thomas, C. Donnelly, R. Wood and L. Alphey, Insect population control using a dominant, repressible, lethal genetic system. *Science* 287 (2000) 2474-2476.
- [35] A. Wächter and L. Biegler, On the implementation of an interior-point filter line-search algorithm for large-scale nonlinear programming. *Math. Progr.* 106 (2006) 25-57. · [Zbl 1134.90542](#)
- [36] T.J.P.H. Walker, P.H. Johnson, L.A. Moreira, I. Iturbe-Ormaetxe, F.D. Frentiu, C.J. McMeniman, Y.S. Leong, Y. Dong, J. Axford, P. Kriesner, et al., The wmel wolbachia strain blocks dengue and invades caged *aedes aegypti* populations. *Nature* 476 (2011) 450.
- [37] H.F. Weinberger, Invariant sets for weakly coupled parabolic and elliptic systems. *Rend. Mat.* 8 (1975) 295-310. · [Zbl 0312.35043](#)
- [38] J. Werren, L. Baldo and M. Clark, Wolbachia: master manipulators of invertebrate biology. *Nat. Rev. Microbiol.* 6 (2008) 741.
- [39] X. Zheng et al., Incompatible and sterile insect techniques combined eliminate mosquitoes. *Nature* 572 (2019) 56-61.

This reference list is based on information provided by the publisher or from digital mathematics libraries. Its items are heuristically matched to zbMATH identifiers and may contain data conversion errors. It attempts to reflect the references listed in the original paper as accurately as possible without claiming the completeness or perfect precision of the matching.