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Optimal control of perfect plasticity. II: Displacement tracking. (English) Zbl 1468.49004
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MSC:

- 49J20 Existence theories for optimal control problems involving partial differential equations
- 49J40 Variational inequalities
- 74C05 Small-strain, rate-independent theories of plasticity (including rigid-plastic and elasto-plastic materials)

Keywords:

optimal control of variational inequalities; perfect plasticity; rate-independent systems; Yosida regularization; reverse approximation

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