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**Gaussian processes centered at their online average, and applications.** (English)

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Summary: We establish various properties of Gaussian processes centered at their online average and discuss their application to goodness-of-fit testing.

**MSC:**

60G15 Gaussian processes

62F05 Asymptotic properties of parametric tests

**Keywords:**

Gaussian processes; online centering; spectral equivalence

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**References:**

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