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Topology optimization for incremental elastoplasticity: a phase-field approach. (English)

Zbl 1455.74074

SIAM J. Control Optim. 59, No. 1, 339-364 (2021).

MSC:

74P15 Topological methods for optimization problems in solid mechanics

74P05 Compliance or weight optimization in solid mechanics

74C05 Small-strain, rate-independent theories of plasticity (including rigid-plastic and elasto-plastic materials)

Cited in 1 Document

Keywords:

first-order optimality condition; regularization; compliance

Full Text: [DOI](#) [arXiv](#)

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