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MSC:

35Q86 PDEs in connection with geophysics
35Q31 Euler equations
35Q35 PDEs in connection with fluid mechanics
86A05 Hydrology, hydrography, oceanography
76U60 Geophysical flows
76B70 Stratification effects in inviscid fluids
76E20 Stability and instability of geophysical and astrophysical flows
35R35 Free boundary problems for PDEs
35A01 Existence problems for PDEs: global existence, local existence, non-existence

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azimuthal flows; general density; cylindrical coordinates; Coriolis force; short-wavelength perturbations

Full Text: DOI

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