

Ji, Zhe; Fu, Lin; Hu, Xiangyu; Adams, Nikolaus

A consistent parallel isotropic unstructured mesh generation method based on multi-phase SPH. (English) [Zbl 1436.65201](#)

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Summary: In this paper, we propose a consistent parallel unstructured mesh generator based on a multi-phase SPH method. A set of physics-motivated modeling equations are developed to achieve the targets of domain decomposition, communication volume optimization and high-quality unstructured mesh generation simultaneously. A unified density field is defined as the target function for both partitioning the geometry and distributing the mesh-vertexes. A multi-phase Smoothing Particle Hydrodynamics (SPH) method is employed to solve the governing equations. All the optimization targets are achieved implicitly and consistently by the particle relaxation procedure without constructing triangulation/tetrahedralization explicitly. The target of communication reduction is achieved by introducing a surface tension model between distinct partitioning sub-domains, which are characterized by colored SPH particles. The resulting partitioning diagram features physically localized sub-domains and optimized interface communication. The target of optimizing the mesh quality is achieved by introducing a tailored equation-of-state (EOS) and a smooth isotropic kernel function. The mesh quality near the interface of neighboring sub-domains is improved by gradually removing the surface-tension force once a steady state is achieved. The proposed method is developed basing on a new parallel environment for multi-resolution SPH to exploit both coarse- and fine-grained parallelism. A set of benchmarks are conducted to verify that all the optimization targets are achieved consistently within the current framework.

MSC:

65N50 Mesh generation, refinement, and adaptive methods for boundary value problems involving PDEs

Cited in **2** Documents

65D18 Numerical aspects of computer graphics, image analysis, and computational geometry

65N55 Multigrid methods; domain decomposition for boundary value problems involving PDEs

76M28 Particle methods and lattice-gas methods

Keywords:

parallel mesh generator; high performance computing; smoothing particle hydrodynamics; domain decomposition

Software:

Intel TBB; Triangle; CUDA; TetGen; Netgen; DualSPHysics

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References:

- [1] Frey, P. J.; George, P.-L., *Mesh Generation: Application to Finite Elements* (2007), ISTE
- [2] Park, M. A.; Krakos, J. A.; Michal, T.; Loseille, A.; Alonso, J. J., *Unstructured grid adaptation: Status, potential impacts, and recommended investments toward CFD Vision 2030* (2016)
- [3] Feng, D.; Tsolaklis, C.; Chernikov, A. N.; Chrisochoides, N. P., *Scalable 3D hybrid parallel Delaunay image-to-mesh conversion algorithm for distributed shared memory architectures*, *Procedia Eng.*, 124, 18-30 (2015)
- [4] Feng, D.; Chernikov, A. N.; Chrisochoides, N. P., *A hybrid parallel Delaunay image-to-mesh conversion algorithm scalable on distributed-memory clusters*, *Proc. Eng.*, 163, 59-71 (2016)
- [5] Slotnick, J.; Khodadoust, A.; Alonso, J.; Darmofal, D.; Gropp, W.; Lurie, E.; Mavriplis, D., *CFD vision 2030 study: a path to revolutionary computational aerosciences* (2014)
- [6] Schöberl, J., *NETGEN An advancing front 2D/3D-mesh generator based on abstract rules*, *Comput. Vis. Sci.*, 1, 1, 41-52 (1997) · [Zbl 0883.68130](#)
- [7] Löhner, R., *Recent advances in parallel advancing front grid generation*, *Arch. Comput. Methods Eng.*, 21, 2, 127-140 (2014) · [Zbl 1349.65667](#)

- [8] Shewchuk, J. R., Delaunay refinement algorithms for triangular mesh generation, *Comput. Geom.*, 22, 1-3, 21-74 (2002) · [Zbl 1016.68139](#)
- [9] Chew, L. P., Guaranteed-quality delaunay meshing in 3D (short version), (Proceedings of the Thirteenth Annual Symposium on Computational Geometry (1997), ACM), 391-393
- [10] Ni, S.; Zhong, Z.; Liu, Y.; Wang, W.; Chen, Z.; Guo, X., Sliver-suppressing tetrahedral mesh optimization with gradient-based shape matching energy, *Comput. Aided Geom. Design*, 52, 247-261 (2017) · [Zbl 1366.65043](#)
- [11] Du, Q.; Faber, V.; Gunzburger, M., Centroidal voronoi tessellations: Applications and algorithms, *SIAM Rev.*, 41, 4, 637-676 (1999) · [Zbl 0983.65021](#)
- [12] Fu, L.; Han, L.; Hu, X. Y.; Adams, N. A., An isotropic unstructured mesh generation method based on a fluid relaxation analogy, *Comput. Methods Appl. Mech. Engrg.*, 350, 396-431 (2019)
- [13] Zhong, Z.; Guo, X.; Wang, W.; Lévy, B.; Sun, F.; Liu, Y.; Mao, W., Particle-based anisotropic surface meshing, *ACM Trans. Graph.*, 32, 4, 99 (2013)
- [14] Fu, L.; Hu, X. Y.; Adams, N. A., Adaptive anisotropic unstructured mesh generation method based on fluid relaxation analogy, *Commun. Comput. Phys.* (2019), in press
- [15] Du, Q.; Wang, D., Tetrahedral mesh generation and optimization based on Centroidal Voronoi Tessellations, *Internat. J. Numer. Methods Engrg.*, 56, 9, 1355-1373 (2003) · [Zbl 1106.74431](#)
- [16] Persson, P.-O., Mesh size functions for implicit geometries and PDE-based gradient limiting, *Eng. Comput.*, 22, 2, 95-109 (2006)
- [17] Meyer, M. D.; Georgel, P.; Whitaker, R. T., Robust particle systems for curvature dependent sampling of implicit surfaces, (International Conference on Shape Modeling and Applications 2005. International Conference on Shape Modeling and Applications 2005, SMI'05 (2005), IEEE), 124-133
- [18] C. Tsolakis, N. Chrisochoides, M.A. Park, A. Loseille, T.R. Michal, Parallel anisotropic unstructured grid adaptation, in: AIAA Scitech 2019 Forum, 2019, p. 1995.
- [19] Chrisochoides, N., Parallel mesh generation, (Numerical Solution of Partial Differential Equations on Parallel Computers (2006), Springer), 237-264 · [Zbl 1097.65122](#)
- [20] Rakotoarivelo, H.; Ledoux, F.; Pommereau, F., Fine-grained locality-aware parallel scheme for anisotropic mesh adaptation, *Proc. Eng.*, 163, 123-135 (2016)
- [21] Lohner, R.; Cebal, J. R., Parallel advancing front grid generation, (International Meshing Roundtable, Sandia National Labs (1999), Citeseer)
- [22] Linardakis, L.; Chrisochoides, N., Delaunay decoupling method for parallel guaranteed quality planar mesh refinement, *SIAM J. Sci. Comput.*, 27, 4, 1394-1423 (2006) · [Zbl 1102.65123](#)
- [23] Loseille, A.; Menier, V.; Alauzet, F., Parallel generation of large-size adapted meshes, *Procedia Eng.*, 124, 57-69 (2015)
- [24] Nave, D.; Chrisochoides, N.; Chew, L. P., Guaranteed-quality parallel Delaunay refinement for restricted polyhedral domains, *Comput. Geom.*, 28, 2-3, 191-215 (2004) · [Zbl 1059.65022](#)
- [25] Galtier, J.; George, P. L., Prepartitioning as a way to mesh subdomains in parallel, (5th International Meshing Roundtable (1996), Citeseer)
- [26] Chew, L. P.; Chrisochoides, N.; Sukup, F., Parallel constrained Delaunay meshing, *ASME Appl. Mech. Div. Publ.*, 220, 89-96 (1997)
- [27] Feng, D.; Chernikov, A. N.; Chrisochoides, N. P., Two-level locality-aware parallel Delaunay image-to-mesh conversion, *Parallel Comput.*, 59, 60-70 (2016)
- [28] Remacle, J.-F.; Bertrand, V.; Geuzaine, C., A two-level multithreaded Delaunay kernel, *Procedia Eng.*, 124, 6-17 (2015)
- [29] Rokos, G.; Gorman, G. J.; Jensen, K. E.; Kelly, P. H., Thread parallelism for highly irregular computation in anisotropic mesh adaptation, (Proceedings of the 3rd International Conference on Exascale Applications and Software (2015), University of Edinburgh), 103-108
- [30] Feng, D.; Chernikov, A. N.; Chrisochoides, N. P., A hybrid parallel Delaunay image-to-mesh conversion algorithm scalable on distributed-memory clusters, *Comput. Aided Des.*, 103, 34-46 (2018)
- [31] Fu, L.; Hu, X. Y.; Adams, N. A., A physics-motivated Centroidal Voronoi Particle domain decomposition method, *J. Comput. Phys.*, 335, 718-735 (2017) · [Zbl 1380.65263](#)
- [32] Forum, M. P., MPI: A Message-Passing Interface StandardTech. Rep. (1994), University of Tennessee: University of Tennessee Knoxville, TN, USA
- [33] Board, O. A.R., OpenMP application program interface vsersion 3.0 (2008), URL <http://www.openmp.org/mp-documents/spec30.pdf>
- [34] Nickolls, J.; Buck, I.; Garland, M.; Skadron, K., Scalable parallel programming with CUDA, *Queue*, 6, 2, 40-53 (2008), URL <http://doi.acm.org/10.1145/1365490.1365500>
- [35] Crespo, A. J.; Domínguez, J. M.; Rogers, B. D.; Gómez-Gesteira, M.; Longshaw, S.; Canelas, R.; Vacondio, R.; Barreiro, A.; García-Feal, O., DualSPHysics: Open-source parallel CFD solver based on Smoothed Particle Hydrodynamics (SPH), *Comput. Phys. Comm.*, 187, 204-216 (2015) · [Zbl 1348.76005](#)
- [36] Plimpton, S., Fast parallel algorithms for short-range molecular dynamics, *J. Comput. Phys.*, 117, 1, 1-19 (1995) · [Zbl 0830.65120](#)
- [37] Incardona, P.; Leo, A.; Zaluzhnyi, Y.; Ramaswamy, R.; Sbalzarini, I. F., OpenFPM: A scalable open framework for particle and particle-mesh codes on parallel computers, *Comput. Phys. Comm.* (2019)

- [38] Ji, Z.; Fu, L.; Hu, X. Y.; Adams, N. A., A new multi-resolution parallel framework for SPH, *Comput. Methods Appl. Mech. Engrg.*, 346, 1156-1178 (2019)
- [39] Fu, L.; Ji, Z.; Hu, X. Y.; Adams, N. A., Parallel fast-neighbor-searching and communication strategy for particle-based methods, *Eng. Comput.*, 36, 3, 899-929 (2019)
- [40] Contreras, G.; Martonosi, M., Characterizing and improving the performance of intel threading building blocks, (Workload Characterization, 2008. IISWC 2008. IEEE International Symposium on (2008), IEEE), 57-66
- [41] Fu, L.; Litvinov, S.; Hu, X. Y.; Adams, N. A., A novel partitioning method for block-structured adaptive meshes, *J. Comput. Phys.*, 341, 447-473 (2017) · [Zbl 1376.76049](#)
- [42] Osher, S.; Sethian, J. A., Fronts propagating with curvature-dependent speed: algorithms based on Hamilton-Jacobi formulations, *J. Comput. Phys.*, 79, 1, 12-49 (1988) · [Zbl 0659.65132](#)
- [43] Piegl, L., On NURBS: a survey, *IEEE Comput. Graph. Appl.*, 11, 1, 55-71 (1991)
- [44] Han, L.; Hu, X.; Adams, N. A., Adaptive multi-resolution method for compressible multi-phase flows with sharp interface model and pyramid data structure, *J. Comput. Phys.*, 262, 131-152 (2014) · [Zbl 1349.76338](#)
- [45] Lorensen, W. E.; Cline, H. E., Marching cubes: A high resolution 3D surface construction algorithm, (*ACM Siggraph Computer Graphics*, Vol. 21, No. 4 (1987), ACM), 163-169
- [46] Brackbill, J.; Kothe, D. B.; Zemach, C., A continuum method for modeling surface tension, *J. Comput. Phys.*, 100, 2, 335-354 (1992) · [Zbl 0775.76110](#)
- [47] Lafaurie, B.; Nardone, C.; Scardovelli, R.; Zaleski, S.; Zanetti, G., Modelling merging and fragmentation in multiphase flows with SURFER, *J. Comput. Phys.*, 113, 1, 134-147 (1994) · [Zbl 0809.76064](#)
- [48] Si, H., TetGen, a Delaunay-based quality tetrahedral mesh generator, *ACM Trans. Math. Softw.*, 41, 2, 11 (2015) · [Zbl 1369.65157](#)
- [49] Starinshak, D. P.; Owen, J.; Johnson, J., A new parallel algorithm for constructing Voronoi tessellations from distributed input data, *Comput. Phys. Commun.*, 185, 12, 3204-3214 (2014) · [Zbl 1360.65076](#)
- [50] Chen, R.; Gotsman, C., Localizing the delaunay triangulation and its parallel implementation, (*Transactions on Computational Science XX* (2013), Springer), 39-55 · [Zbl 1406.68114](#)
- [51] Ji, Z.; Fu, L.; Hu, X. Y.; Adams, N. A., A Lagrangian Inertial Centroidal Voronoi Particle method for dynamic load balancing in particle-based simulations, *Comput. Phys. Comm.*, 239, 53-63 (2019)
- [52] Fu, L.; Ji, Z., An optimal particle setup method with Centroidal Voronoi Particle dynamics, *Comput. Phys. Comm.*, 234, 72-92 (2019)
- [53] Adami, S.; Hu, X.; Adams, N. A., A new surface-tension formulation for multi-phase SPH using a reproducing divergence approximation, *J. Comput. Phys.*, 229, 13, 5011-5021 (2010) · [Zbl 1346.76161](#)
- [54] Meyerhenke, H.; Monien, B.; Schamberger, S., Graph partitioning and disturbed diffusion, *Parallel Comput.*, 35, 10-11, 544-569 (2009)
- [55] Turk, G.; Levoy, M., Zippered polygon meshes from range images, (*Proceedings of the 21st Annual Conference on Computer Graphics and Interactive Techniques* (1994), ACM), 311-318
- [56] Barnes, E.; Sloane, N., The optimal lattice quantizer in three dimensions, *SIAM J. Algebr. Discrete Methods*, 4, 1, 30-41 (1983) · [Zbl 0509.52010](#)
- [57] Hoehn, B. R.; Oster, P.; Tobie, T.; Michaelis, K., Test methods for gear lubricants, *Goriva i maziva*, 47, 2, 141-152 (2008)
- [58] Löhner, R.; Onate, E., An advancing front point generation technique, *Commun. Numer. Methods. Eng.*, 14, 12, 1097-1108 (1998) · [Zbl 0920.65071](#)

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