Cornejo, María Eugenia; **Medina, Jesús**; **Ramírez-Poussa, Eloisa**

Adjoint triples and residuated aggregators. (English) Zbl 1432.03106

Laurent, Anne (ed.) et al., Information processing and management of uncertainty in knowledge-based systems. 15th international conference, IPMU 2014, Montpellier, France, July 15–19, 2014. Proceedings. Part III. Cham: Springer. Commun. Comput. Inf. Sci. 444, 345-354 (2014).

Summary: Several domains, such as fuzzy logic programming, formal concept analysis and fuzzy relation equations, consider basic operators which need to have associated residuated implications. Adjoint triples are formed by operators satisfying weak properties, usefully used in these domains. This paper presents the comparison of these triples with other general operators considered in these frameworks.

For the entire collection see [Zbl 1385.68008].

MSC:

03E72 Theory of fuzzy sets, etc.
03G25 Other algebras related to logic
06A15 Galois correspondences, closure operators (in relation to ordered sets)

Keywords:

adjoint triples; implication triples; u-norms; uninorms

Full Text: DOI

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