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Modeling hypersonic entry with the fully-implicit Navier-Stokes (FIN-S) stabilized finite element flow solver. (English) Zbl 1391.76340
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Summary: In this paper, we present a novel scheme for modeling the hypersonic atmospheric entry of large vehicles with an ablative thermal protection system. The Favre-averaged thermochemical nonequilibrium Navier-Stokes equations with Spalart-Allmaras turbulence closure, thermodynamic, chemical kinetic, and quasi-steady ablation model are presented. The numerical method is based on a streamline upwind Petrov-Galerkin (SUPG) stabilized finite element formulation. The formulation and implementation of the finite element approximation are discussed in detail. The performance of the scheme is investigated through a series of increasingly complex applications, culminating in the simulation of a three-dimensional ablating heatshield in transitioning flow.

MSC:

76M10 Finite element methods applied to problems in fluid mechanics

76K05 Hypersonic flows

76D05 Navier-Stokes equations for incompressible viscous fluids

Cited in **3** Documents

Keywords:

[stabilized finite elements](#); [compressible flow](#); [hypersonic flow](#); [reentry](#); [surface ablation](#)

Software:

[Spalart-Allmaras](#); [PETSc](#); [MASA](#); [libMesh](#)

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