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**Mode-sum construction of the two-point functions for the Stueckelberg vector fields in the Poincaré patch of de Sitter space.** (English) Zbl 1294.81135  
*J. Math. Phys.* 55, No. 6, 062301, 21 p. (2014).

Summary: We perform canonical quantization of the Stueckelberg Lagrangian for massive vector fields in the conformally flat patch of de Sitter space in the Bunch-Davies vacuum and find their Wightman two-point functions by the mode-sum method. We discuss the zero-mass limit of these two-point functions and their limits where the Stueckelberg parameter  $\xi$  tends to zero or infinity. It is shown that our results reproduce the standard flat-space propagator in the appropriate limit. We also point out that the classic work of *B. Allen* and *T. Jacobson* [*Commun. Math. Phys.* 103, 669–692 (1986; [Zbl 0632.53060](#))] for the two-point function of the Proca field and a recent work by *N. C. Tsamis* and *R. P. Woodard* [*J. Math. Phys.* 48, No. 5, 052306, 14 p. (2007; [Zbl 1144.81417](#))] for that of the transverse vector field are two limits of our two-point function, one for  $\xi \rightarrow \infty$  and the other for  $\xi \rightarrow 0$ . Thus, these two works are consistent with each other, contrary to the claim by the latter authors.

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**MSC:**

- [81T20](#) Quantum field theory on curved space or space-time backgrounds
- [81T70](#) Quantization in field theory; cohomological methods
- [70S05](#) Lagrangian formalism and Hamiltonian formalism in mechanics of particles and systems
- [81V22](#) Unified quantum theories
- [81R40](#) Symmetry breaking in quantum theory
- [83F05](#) Relativistic cosmology

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**Keywords:**

[Wightman two-point functions](#)

**Full Text:** [DOI](#) [arXiv](#)

**References:**

- [1] Allen, B.; Jacobson, T., Vector two-point functions in maximally symmetric spaces, *Commun. Math. Phys.*, 103, 669, (1986) · [Zbl 0632.53060](#) · [doi:10.1007/BF01211169](#)
- [2] Proca, A., Sur les équations fondamentales des particules élémentaires, *C. R. Acad. Sci.*, 202, 1490, (1936) · [Zbl 62.1001.02](#)
- [3] Tsamis, N. C.; Woodard, R. P., Maximally symmetric vector propagator, *J. Math. Phys.*, 48, 052306, (2007) · [Zbl 1144.81417](#) · [doi:10.1063/1.2738361](#)
- [4] Stueckelberg, E. C. G., Die Wechselwirkungskräfte in der Elektrodynamik und in der Feldtheorie der Kernkräfte. Teil II und III, *Helv. Phys. Acta*, 11, 299, (1938) · [Zbl 64.1492.03](#) · [doi:10.5169/seals-110855](#)
- [5] Schomblond, C.; Spindel, P., Propagateurs des champs spinoriels et vectoriels dans l'univers de de Sitter, *Bull. Cl. Sci. Acad. Roy. Belg.*, LXII, 124-134, (1976) · [Zbl 0329.53012](#)
- [6] Higuchi, A., Quantization of scalar and vector fields inside the cosmological event horizon and its application to the Hawking effect, *Class. Quantum Grav.*, 4, 721, (1987) · [doi:10.1088/0264-9381/4/3/029](#)
- [7] Gazeau, J.-P.; Takook, M. V., Massive' vector field in de Sitter space, *J. Math. Phys.*, 41, 5920, (2000) · [Zbl 0978.81062](#) · [doi:10.1063/1.1287641](#)
- [8] Cotăescu, I. I., Polarized vector bosons on the de Sitter expanding universe, *Gen. Rel. Grav.*, 42, 861, (2010) · [Zbl 1188.83043](#) · [doi:10.1007/s10714-009-0886-7](#)
- [9] Itzykson, C.; Zuber, J. B., *Quantum Field Theory*, (1980), McGraw-Hill: McGraw-Hill, New York · [Zbl 0453.05035](#)
- [10] See for NIST Digital Library of Mathematical Functions.
- [11] Candelas, P.; Raine, D. J., General-relativistic quantum field theory: An exactly soluble model, *Phys. Rev. D*, 12, 965, (1975) · [doi:10.1103/PhysRevD.12.965](#)
- [12] Youssef, A., Infrared behavior and gauge artifacts in de Sitter spacetime: The photon field, *Phys. Rev. Lett.*, 107, 021101, (2011) · [doi:10.1103/PhysRevLett.107.021101](#)
- [13] Smirnov, V. A., *Evaluating Feynman Integrals*, (2005), Springer: Springer, Berlin/Heidelberg

- [14] Schwinger, J. S., Field theory commutators, *Phys. Rev. Lett.*, 3, 296, (1959) · doi:10.1103/PhysRevLett.3.296
- [15] Boulware, D. G.; Deser, S., Stress-Tensor commutators and Schwinger terms, *J. Math. Phys.*, 8, 1468, (1967) · doi:10.1063/1.1705368
- [16] Jacob, G.; Stech, B., Commutators and Lorentz covariance, *Z. Phys.*, 239, 379, (1970) · doi:10.1007/BF01401193
- [17] Dashen, R. F.; Lee, S. Y., Existence of the covariant time-ordered product of currents, *Phys. Rev.*, 187, 2017, (1969) · doi:10.1103/PhysRev.187.2017
- [18] Nutbrown, D. A., Simple derivation of Seagull terms for propagator functions, *Phys. Rev. D*, 3, 2981, (1971) · doi:10.1103/PhysRevD.3.2981
- [19] Gross, D. J.; Jackiw, R., Construction of covariant and gauge invariant  $T^*$  products, *Nucl. Phys. B*, 14, 269, (1969) · doi:10.1016/0550-3213(69)90207-7
- [20] Brown, S. G., Covariance and the cancellation of Schwinger and Seagull terms in applications of current algebras, *Phys. Rev.*, 158, 1444, (1967) · doi:10.1103/PhysRev.158.1444
- [21] Kahya, E. O.; Woodard, R. P., Charged scalar self-mass during inflation, *Phys. Rev. D*, 72, 104001, (2005) · doi:10.1103/PhysRevD.72.104001
- [22] Higuchi, A.; Lee, Y. C., How to use retarded Green's functions in de Sitter spacetime, *Phys. Rev. D*, 78, 084031, (2008) · doi:10.1103/PhysRevD.78.084031
- [23] Higuchi, A.; Lee, Y. C.; Nicholas, J. R., More on the covariant retarded Green's function for the electromagnetic field in de Sitter spacetime, *Phys. Rev. D*, 80, 107502, (2009) · doi:10.1103/PhysRevD.80.107502
- [24] Kahya, E. O.; Woodard, R. P., One loop corrected mode functions for SQED during inflation, *Phys. Rev. D*, 74, 084012, (2006) · doi:10.1103/PhysRevD.74.084012
- [25] Prokopec, T.; Tsamis, N. C.; Woodard, R. P., Two loop scalar bilinears for inflationary SQED, *Class. Quantum Grav.*, 24, 201-230, (2007) · Zbl 1133.83341 · doi:10.1088/0264-9381/24/1/011
- [26] Prokopec, T.; Tsamis, N. C.; Woodard, R. P., Two loop stress-energy tensor for inflationary scalar electrodynamics, *Phys. Rev. D*, 78, 043523, (2008) · doi:10.1103/PhysRevD.78.043523
- [27] Coleman, S. R.; Weinberg, E. J., Radiative corrections as the origin of spontaneous symmetry breaking, *Phys. Rev. D*, 7, 1888-1910, (1973) · doi:10.1103/PhysRevD.7.1888
- [28] Allen, B., Phase transitions in de Sitter space, *Nucl. Phys. B*, 226, 228, (1983) · doi:10.1016/0550-3213(83)90470-4
- [29] Prokopec, T.; Tsamis, N.; Woodard, R., Stochastic inflationary scalar electrodynamics, *Ann. Phys.*, 323, 1324-1360, (2008) · Zbl 1151.81030 · doi:10.1016/j.aop.2007.08.008
- [30] Nielsen, N., On the gauge dependence of spontaneous symmetry breaking in gauge theories, *Nucl. Phys. B*, 101, 173, (1975) · doi:10.1016/0550-3213(75)90301-6
- [31] Aitchison, I.; Fraser, C., Gauge invariance and the effective potential, *Ann. Phys.*, 156, 1, (1984) · Zbl 1216.81109 · doi:10.1016/0003-4916(84)90209-4
- [32] Johnston, D., Nielsen identities in the 't Hooft gauge, *Nucl. Phys. B*, 253, 687, (1985) · doi:10.1016/0550-3213(85)90553-X
- [33] Tsamis, N. C.; Woodard, R. P., The structure of perturbative quantum gravity on a de Sitter background, *Commun. Math. Phys.*, 162, 217-248, (1994) · Zbl 0809.53084 · doi:10.1007/BF02102015
- [34] Bičák, J.; Krtouš, P., Accelerated sources in de Sitter space-time and the insufficiency of retarded fields, *Phys. Rev. D*, 64, 124020, (2001) · doi:10.1103/PhysRevD.64.124020
- [35] Woodard, R. P.; Liu, J. T.; Duff, M. J.; Stelle, K. S.; Woodard, R. P., De Sitter breaking in field theory, *Proceedings of Deserfest: A Celebration of the Life and Works of Stanley Deser*, Ann Arbor, USA, 3-5 April 2004, 339, (2006), World Scientific Publishing: World Scientific Publishing, Singapore · Zbl 1126.81047
- [36] Faci, S.; Huguet, E.; Renaud, J., Conformal use of retarded Green's functions for the Maxwell field in de Sitter space, *Phys. Rev. D*, 84, 124050, (2011) · doi:10.1103/PhysRevD.84.124050
- [37] Fröb, M. B.; Roura, A.; Verdaguer, E., One-loop gravitational wave spectrum in de Sitter spacetime, *JCAP*, 1208, 009, (2012) · doi:10.1088/1475-7516/2012/08/009
- [38] Tanaka, T.; Urakawa, Y., Loops in inflationary correlation functions, *Class. Quantum Grav.*, 30, 233001, (2013) · Zbl 1284.83013 · doi:10.1088/0264-9381/30/23/233001
- [39] Marolf, D.; Morrison, I. A., The IR stability of de Sitter: Loop corrections to scalar propagators, *Phys. Rev. D*, 82, 105032, (2010) · doi:10.1103/PhysRevD.82.105032
- [40] Higuchi, A.; Marolf, D.; Morrison, I. A., On the equivalence between Euclidean and in-in formalisms in de Sitter QFT, *Phys. Rev. D*, 83, 084029, (2011) · doi:10.1103/PhysRevD.83.084029
- [41] Korai, Y.; Tanaka, T., QFT in the flat chart of de Sitter space, *Phys. Rev. D*, 87, 024013, (2013) · doi:10.1103/PhysRevD.87.024013
- [42] Bailey, W. N., Some infinite integrals involving Bessel functions, *Proc. London Math. Soc.*, s2-s40, 37, (1936) · Zbl 61.0398.01 · doi:10.1112/plms/s2-40.1.37

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