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Convergence of solutions to Cahn-Hilliard equation. (English) Zbl 0936.35032
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The authors show the convergence to an equilibrium as $t \rightarrow \infty$ of solutions to the Cahn-Hilliard equation

$$u_t = \Delta(-\varepsilon^2 \Delta u + W_u(u)), \quad u(0) = u_0 \text{ in } \Omega; \quad \frac{\partial u}{\partial \nu} = 0 = \frac{\partial}{\partial \nu}(-\varepsilon^2 \Delta u + W_u(u)) \text{ on } \partial\Omega.$$

W is assumed to be analytic in u , which allows them to prove a Łojasiewicz inequality for the associated gradient flow in $W^{-1,2}(\Omega)$, which they use in turn to prove the convergence for the associated class of nonlinear parabolic equations by a method modeled by *L. Simon* [*Ann. Math.*, II. Ser. 118, 525-571 (1983; [Zbl 0549.35071](#))]. The paper also contains an existence and uniqueness result with the appropriate regularity for solutions providing the background for the study of the asymptotic behaviour.

Reviewer: [Marianne Korten \(Warszawa\)](#)

MSC:

- [35B40](#) Asymptotic behavior of solutions to PDEs
- [35K60](#) Nonlinear initial, boundary and initial-boundary value problems for linear parabolic equations
- [35K35](#) Initial-boundary value problems for higher-order parabolic equations

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Keywords:

[Łojasiewicz inequality](#); [convergence to equilibria](#)

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