

**Albeverio, Sergio; Cianci, Roberto; Khrennikov, Andrew**

**On the Fourier transform and the spectral properties of the  $p$ -adic momentum and Schrödinger operators.** (English) [Zbl 0927.46060](#)

*J. Phys. A, Math. Gen.* 30, No. 16, 5767-5784 (1997).

The authors continue the study of the  $p$ -adic model of quantum mechanics initiated in their previous papers [*S. Albeverio, A. Khrennikov, J. Phys. A, Math. Gen.* 29, 5515-5527 (1996; [Zbl 0903.46073](#)); *S. Albeverio, R. Cianci, A. Khrennikov, J. Phys. A, Math. Gen.* 30, 881-889 (1997)]. In particular, a version of the Fourier transform is introduced, which is adapted to the spaces used in the paper,  $L_2$ -spaces with respect to the  $p$ -adic Gaussian distribution.

In the momentum representation the analogue of the momentum operator is similar to the position operator of the coordinate representation, which was studied earlier. As a result, spectral properties of the momentum operator are investigated. A possible physical meaning of the results is discussed, in particular the idea of a  $p$ -adic description of the finite exactness of measurement.

For another recent  $p$ -adic model of quantum mechanics, which is closely related to classical constructions of  $p$ -adic analysis, see the paper by the reviewer [*A. N. Kochubei, J. Phys. A, Math. Gen.* 29, 6375-6378 (1996; [Zbl 0905.46051](#))].

Reviewer: [Anatoly N.Kochubei \(Kiev\)](#)

**MSC:**

- [46S10](#) Functional analysis over fields other than  $\mathbb{R}$  or  $\mathbb{C}$  or the quaternions; non-Archimedean functional analysis
- [81S05](#) Commutation relations and statistics as related to quantum mechanics (general)
- [81P15](#) Quantum measurement theory, state operations, state preparations
- [11S80](#) Other analytic theory (analogues of beta and gamma functions,  $p$ -adic integration, etc.)
- [81Q05](#) Closed and approximate solutions to the Schrödinger, Dirac, Klein-Gordon and other equations of quantum mechanics

Cited in **8** Documents

**Keywords:**

$p$ -adic quantum mechanics;  $p$ -adic Fourier transform; momentum operator; position operator; measurement;  $p$ -adic Gaussian distribution

**Full Text:** [DOI](#)