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MSC:

- 35R30 Inverse problems for PDEs
- 35B35 Stability in context of PDEs
- 35J30 Higher-order elliptic equations
- 35P25 Scattering theory for PDEs
- 78A46 Inverse problems (including inverse scattering) in optics and electromagnetic theory

Keywords:

resolvent estimate; compactly supported potential

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