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Local saddles of relaxed averaged alternating reflections algorithms on phase retrieval.

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Wirtinger Flow; FTVd

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