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**Adaptive variational model for contrast enhancement of low-light images.** (English)

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**MSC:**

68T45 Machine vision and scene understanding

65K10 Numerical optimization and variational techniques

94A08 Image processing (compression, reconstruction, etc.) in information and communication theory

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contrast enhancement; image enhancement; adaptive variational model; nonuniform illumination; low-light images

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