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**Analysis of turbulence characteristics in a temporal dense gas compressible mixing layer using direct numerical simulation.** (English) [Zbl 07192803](#)

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Summary: This study investigates the effects of a Bethe-Zel'dovich-Thompson (BZT) dense gas (FC-70) on the development of a turbulent compressible mixing layer at a convective Mach number  $M_c = 1.1$ . Three-dimensional direct numerical simulations are performed with both FC-70 and air. The initial thermodynamic state for FC-70 lies inside the inversion region where the fundamental derivative of gas dynamics ( $\Gamma$ ) becomes negative. The complex Martin-Hou thermodynamic equation of state is used to reproduce thermodynamic peculiarities of the BZT dense gas (DG). The unstable growth phase in the mixing layer development shows an increase of  $xy$ -turbulent stress tensors in DG compared to perfect gas (PG). The following self-similar period has been carefully defined from the time evolution of the integrated streamwise production and transport terms. During the self-similar stage, DG and PG mixing layers at  $M_c = 1.1$  display close values of the momentum thickness growth rate, which seems similarly affected by the well-known compressibility-related reduction for PG. The same mechanisms are at stake, related to the reduction of pressure-strain terms. Turbulent kinetic energy (TKE) spectra show a slower decrease of TKE at small scales for DG compared with PG. The filtered kinetic energy equation balance developed by *H. Aluie* [Physica D 247, No. 1, 54–65 (2013; [Zbl 1308.76133](#))] is applied for the first time to a compressible mixing layer. The equation is reshaped to better account for TKE transport across the mixing layer. This new formulation brings out the role played by  $\Sigma_t$ , the pressure strengths power. A detailed comparison of the contributions to the filtered TKE equation is provided for both PG and DG mixing layers.

**MSC:**

76 Fluid mechanics

**Keywords:**

compressible turbulence; shear layer turbulence; turbulence simulation

**Full Text:** [DOI](#)

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