Ko, Jung Mi; **Kim, Yong Chan**
Fuzzy connections on adjoint triples. (English) Zbl 07181611
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Summary: In this paper, we introduce the notion of residuated and Galois connections on adjoint triples and investigate their properties. Using the properties of residuated and Galois connections, we solve fuzzy relation equations and give their examples.

MSC:

03E72 Theory of fuzzy sets, etc.
03G10 Logical aspects of lattices and related structures
06A15 Galois correspondences, closure operators (in relation to ordered sets)
54F05 Linearly ordered topological spaces, generalized ordered spaces, and partially ordered spaces

Keywords:

adjoint triples; residuated connections; Galois connections; fuzzy relational erosion(dilation); fuzzy closure (interior) operator

Full Text: DOI

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