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Constrained implementation. (English) Zbl 1422.91233

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Summary: Consider a society with two sectors (issues or objects) that faces a design problem. Suppose that the sector-2 dimension of the design problem is fixed and represented by a mechanism Γ^2 , and that the designer operates under this constraint for institutional reasons. A sector-1 mechanism Γ^1 constrained implements a social choice rule φ in Nash equilibrium if for each profile of agents' preferences, the set of (pure) Nash equilibrium outcomes of the mechanism $\Gamma^1 \times \Gamma^2$ played by agents with those preferences always coincides with the recommendations made by φ for that profile. If this mechanism design exercise could be accomplished, φ would be constrained implementable. We show that *constrained monotonicity*, a strengthening of (Maskin) monotonicity, is a necessary condition for constrained implementation. When there are more than two agents, and when the designer can use the private information elicited from agents via Γ^2 to make a socially optimal decision for sector 1, constrained monotonicity, combined with an auxiliary condition, is sufficient. This sufficiency result does *not* rule out any kind of complementarity between the two sectors.

MSC:

[91B14](#) Social choice

[91A40](#) Other game-theoretic models

Keywords:

[constrained implementation](#); [mechanism design](#); [Nash implementation](#)

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References:

- [1] Abreu, D.; Matsushima, H., Virtual implementation in iteratively undominated strategies: complete information, *Econometrica*, 60, 993-1008, (1992) · [Zbl 0766.90002](#)
- [2] Diamantaras, D.; Wilkie, S., A generalization of Kaneko's ratio equilibrium for economies with private and public goods, *J. Econ. Theory*, 62, 499-512, (1994) · [Zbl 0801.90016](#)
- [3] Dutta, B.; Sen, A., A necessary and sufficient condition for two-person Nash implementation, *Rev. Econ. Stud.*, 58, 121-128, (1991) · [Zbl 0717.90005](#)
- [4] Hayashi, T.; Lombardi, M., Implementation in partial equilibrium, *J. Econ. Theory*, 169, 13-34, (2017) · [Zbl 1400.91165](#)
- [5] Hayashi, T.; Sakai, T., Nash implementation of competitive equilibria in the job-matching market, *Int. J. Game Theory*, 38, 453-467, (2009) · [Zbl 1211.91178](#)
- [6] Kaneko, M., The ratio equilibrium and a voting game in a public goods economy, *J. Econ. Theory*, 16, 123-136, (1977) · [Zbl 0399.90019](#)
- [7] Jackson, M. O., Implementation in undominated strategies: a look at bounded mechanisms, *Rev. Econ. Stud.*, 59, 757-775, (1992) · [Zbl 0771.90004](#)
- [8] Jackson, M. O., A crash course in implementation theory, *Soc. Choice Welf.*, 18, 655-708, (2001) · [Zbl 1069.91557](#)
- [9] Lombardi, M.; Yoshihara, N., A full characterization of Nash implementation with strategy space reduction, *Econ. Theory*, 54, 131-151, (2013) · [Zbl 1284.91023](#)
- [10] Maskin, E., Nash equilibrium and welfare optimality, *Rev. Econ. Stud.*, 66, 23-38, (1999) · [Zbl 0956.91034](#)
- [11] Maskin, E.; Sjöström, T., Implementation theory, (Arrow, K.; Sen, A. K.; Suzumura, K., *Handbook of Social Choice and Welfare*, (2002), Elsevier Science: Elsevier Science Amsterdam), 237-288
- [12] Moore, J.; Repullo, R., Nash implementation: a full characterization, *Econometrica*, 58, 1083-1100, (1990) · [Zbl 0731.90009](#)
- [13] Ollár, M.; Penta, A., Full implementation and belief restrictions, *Am. Econ. Rev.*, 107, 2243-2277, (2017)
- [14] Schmeidler, D., Walrasian analysis via strategic outcome functions, *Econometrica*, 48, 1585-1593, (1980) · [Zbl 0457.90014](#)
- [15] Sjöström, T., On the necessary and sufficient conditions for Nash implementation, *Soc. Choice Welf.*, 8, 333-340, (1991) · [Zbl 0734.90007](#)
- [16] Svensson, L.-G., Nash implementation of competitive equilibria in a model with indivisible goods, *Econometrica*, 59, 869-877,

(1991) · Zbl 0748.90004

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