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Spherical symmetry as a test case for unconstrained hyperboloidal evolution. II: Gauge conditions. (English) Zbl 1386.83022

Classical Quantum Gravity 35, No. 4, Article ID 045014, 31 p. (2018).

MSC:

83C05 Einstein's equations (general structure, canonical formalism, Cauchy problems)
83-08 Computational methods for problems pertaining to relativity and gravitational theory
83C25 Approximation procedures, weak fields in general relativity and gravitational theory
83C57 Black holes
83C10 Equations of motion in general relativity and gravitational theory

Keywords:

hyperboloidal initial value problem; asymptotic structure; numerical relativity; conformal compactification; gauge conditions

Software:

xAct

Full Text: DOI

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