Lee, Jung Rye; **Park, Choonkil**; **Shin, Dong Yun**; **Yun, Sungsik**
Set-valued quadratic functional equations. (English) Zbl 1453.39022
Result. Math. 72, No. 1-2, 665-677 (2017).

Summary: In this paper, we introduce set-valued quadratic functional equations and prove the Hyers-Ulam stability of the set-valued quadratic functional equations by using the fixed point method.

MSC:

39B52 Functional equations for functions with more general domains and/or ranges
39B82 Stability, separation, extension, and related topics for functional equations
47H04 Set-valued operators
47H10 Fixed-point theorems

Cited in **4** Documents

Keywords:

Hyers-Ulam stability; set-valued quadratic functional equation; fixed point

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