

Lara, Danielle; Marchesi, Simone; Martins, Renato Vidal
Curves with canonical models on scrolls. (English) Zbl 1357.14040
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Throughout, let C be a curve (i.e., an integral, complete, one-dimensional scheme) over an algebraically closed field of arithmetic genus g . Let $C' \subseteq \mathbb{P}^{g-1}$ be its canonical model which is defined by the global sections of the dualizing sheaf of C . It is well-known so far that properties on trigonal Gorenstein curves can be deduced whenever its canonical model is contained in a surface scroll; e.g. [*K.-O. Stöhr*, J. Pure Appl. Algebra 135, No. 1, 93–105 (1999; [Zbl 0940.14018](#))], [*R. Rosa and K.-O. Stöhr*, J. Pure Appl. Algebra 174, No. 2, 187–205 (2002; [Zbl 1059.14038](#))].

In this paper the authors study the case where C is non-Gorenstein and C' is contained in a scroll surface. Here the concepts “nearly Gorenstein” and “arithmetically normal” become relevant according respectively to Theorems 5.10 and 4 in [*S. L. Kleiman and R. V. Martins*, Geom. Dedicata 139, 139–166 (2009; [Zbl 1172.14019](#))]. Moreover, as looking at for examples, they consider rational monomial curves and show that for such a curve its canonical model is contained in a scroll surface if and only if the curve is trigonal. This leads to the question when a nonhyperelliptic curve can be characterized by its canonical model; in fact, this is worked out for the case of a nonhyperelliptic curve with at most one unbranched singular point. Finally they generalize some results in [*F.-O. Schreyer*, Math. Ann. 275, 105–137 (1986; [Zbl 0578.14002](#))].

Reviewer: [Fernando Torres \(Campinas\)](#)

MSC:

- [14H20](#) Singularities of curves, local rings
- [14H45](#) Special algebraic curves and curves of low genus
- [14H51](#) Special divisors on curves (gonality, Brill-Noether theory)

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Keywords:

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