

**Walsh, Timothy R.**

**Counting maps on doughnuts.** (English) [Zbl 1301.05179](#)  
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Summary: How many maps with  $V$  vertices and  $E$  edges can be drawn on a doughnut with  $G$  holes? I solved this problem for doughnuts with up to 10 holes, and my colleagues *A. Giorgetti* and *A. Mednykh* [*Ars Math. Contemp.* 4, No. 2, 351–361 (2011; [Zbl 1237.05104](#))] counted maps by number of edges alone on doughnuts with up to 11 holes. This expository paper outlines, in terms meant to be understandable by a non-specialist, the methods we used and those used by other researchers to obtain the results upon which our own research depends.

**MSC:**

**05C30** Enumeration in graph theory

Cited in **3** Documents

**Keywords:**

rooted maps; unrooted maps; orientable surfaces; exact enumeration; generating functions; orbifolds

**Software:**

Maple

**Full Text:** [DOI](#)

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