Anello, Giovanni; **Cordaro, Giuseppe**
On the asymptotic behavior of certain solutions of the Dirichlet problem for the equation
$-\Delta_p u = \lambda|u|^{q-2}u$. (English) ⟨Zbl 1281.35013⟩
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Summary: Let $p > 1$. We study the behavior of certain positive and nodal solutions of the problem

$$\begin{cases} -\Delta_p u = \lambda|u|^{q-2} & \text{in } \Omega, \\ u = 0 & \text{on } \partial\Omega, \end{cases}$$

on varying of the parameters $\lambda > 0$ and $q > 1$.

MSC:

35J20	Variational methods for second-order elliptic equations
35J25	Boundary value problems for second-order elliptic equations
35B40	Asymptotic behavior of solutions to PDEs
35B09	Positive solutions to PDEs

Cited in **1** Document

Keywords:

elliptic boundary value problems; positive solutions; nodal solutions; minimal energy; asymptotic behavior; variational methods

Full Text: DOI

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