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Formal verification of a modern SAT solver by shallow embedding into Isabelle/HOL. (English) [Zbl 1208.68205](#)

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Summary: We present a formalization and a formal total correctness proof of a MiniSAT-like SAT solver within the system Isabelle/HOL. The solver is based on the DPLL procedure and employs most state-of-the-art SAT solving techniques, including the conflict-guided backjumping, clause learning, and the two-watched unit propagation scheme. A shallow embedding into Isabelle/HOL is used and the solver is expressed as a set of recursive HOL functions. Based on this specification, the Isabelle's built-in code generator can be used to generate executable code in several supported functional languages (Haskell, SML, and OCaml). The SAT solver implemented in this way is, to our knowledge, the first fully formally and mechanically verified modern SAT solver.

MSC:

68T20 Problem solving in the context of artificial intelligence (heuristics, search strategies, etc.)

Cited in **11** Documents

68Q60 Specification and verification (program logics, model checking, etc.)

Keywords:

formal program verification; SAT problem; DPLL procedure; Isabelle

Software:

Archive Formal Proofs; BerkMin; Chaff; Isabelle; Isabelle/HOL; MiniSat; OCaml; SATO; SAT Solver Verification

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