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**On the cryptographic value of the  $q^{\text{th}}$  root problem.** (English) [Zbl 1014.94553](#)

Varadharajan, Vijay (ed.) et al., Information and communication security. 2nd international conference, ICICS '99, Sydney, Australia, November 9-11, 1999. Proceedings. Berlin: Springer. Lect. Notes Comput. Sci. 1726, 135-142 (1999).

Summary: The authors show that, for a prime  $q$  and a group  $G$ , if  $\text{ord}(G) = q^k r$ ,  $k > 1$ , and  $r$  is smooth, then finding a  $q$ th root in  $G$  is equivalent to the discrete logarithm problem over  $G$  (note that the discrete logarithm problem over the group  $G$  reduces to the discrete logarithm problem over a subgroup of order  $q$  – see *S. Pohlig* and *M. Hellman* [*IEEE Trans. Inf. Theory* 24, 106-110 (1978; [Zbl 0375.68023](#))]. Several publications describe techniques for computing  $q$ th roots. All have the stated or implied requirement of computing discrete logarithms in a subgroup of order  $q$ .

The emphasis here will be on demonstrating that with a fairly general  $q$ th root oracle, discrete logarithms in a subgroup of order  $q$  may be found, describing the cryptographic significance of this problem, and in introducing two new public key signature schemes based on it.

For the entire collection see [[Zbl 0931.00051](#)].

**MSC:**

[94A60](#) Cryptography

[11Y16](#) Number-theoretic algorithms; complexity

Cited in 1 Document

**Keywords:**

discrete logarithms; subgroup of order  $q$ ; cryptographic significance; public key signature schemes