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**Remarks concerning a method for accelerating the convergence of sequences.** (English)

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Rev. Anal. Numér. Théor. Approx. 23, No. 1, 79-87 (1994).

The main result may be presented as follows. Denote the differences of a sequence  $a(n)$  ( $n \geq 0$ ) by  $\Delta(a||r|n)$ , so that  $\Delta(a||0|n) = a(n)$ ,  $\Delta(a||1|n) = a(n+1) - a(n)$  and so on. Let  $S(n)$  ( $n \geq 0$ ) be a monotonic sequence and  $a(n)$  ( $n \geq 0$ ) be an auxiliary sequence for which, as  $n$  increases,  $\lim \Delta(a||p-1|n) = L$  exists and is finite,  $p \geq 1$  being fixed. Set  $B(a, S||p, k|n) = \Delta(a||p|n) / \Delta(S||1|k+n)$ ,  $k \geq 0$  also being fixed. If, as  $n$  increases,  $\lim B(a, S||p, k|n)$  is finite and nonzero then  $S = \lim S(n)$  exists and, setting  $T(n) = S(n) + \{L - \Delta(a||p-1|n-k)\} / B(a, S||p, k|n)$ , the ratio  $\{S - T(n)\} / \{S - S(n)\}$  tends, as  $n$  increases, to zero.

Reviewer: P.Wynn (Mexico)

**MSC:**

65B05 Extrapolation to the limit, deferred corrections

40A05 Convergence and divergence of series and sequences

**Keywords:**

monotonic sequences; convergence test; convergence acceleration